

ICHEP2002, 26 July, 2002, Amsterdam

Project SANC (former CalcPHEP):
Support of Analytic and Numeric calculations for experiments at Colliders

D. Bardin

Laboratory of Nuclear Problems, Joint Institute for Nuclear Research

OUTLINE

- 1. SANC project and its roots**
- 2. Basic notions**
- 3. Present status of the project**
- 4. Concluding remarks**

1. SANC project and its roots

People:

D. Bardin, L. Kalinovskaya, P. Christova, A. Andonov, G. Nanava – LNP, JINR;
 S. Bondarenko – BTL, JINR; G. Passarino – Torino University.

In collaboration on MC issues with:

S. Jadach, Z. Was – INF Krakow and B.F.L. Ward – Knoxville University.

Goal:

creation of a software product for computation of pseudo- and realistic observables
 with one-loop precision for the processes of elementary particle interactions:

$1 \rightarrow 2$, $1 \rightarrow 3$, $2 \rightarrow 2$, $1 \rightarrow 4$, $2 \rightarrow 3$...

Application: LHC, Linacs.

Roots:

Codes aimed at a theoretical support of HEP experiments;
 ZFITTER and the others...

Book DB and G. Passarino:

The Standard Model in the Making, OUP 1999;
 numerous book-supporting form2-codes...



2. Basic notions

- The Standard Model (SM) Lagrangian in the R_ξ gauge:

$$\mathcal{L} = \mathcal{L}(\text{IPS of 25 parameters, fields, } \xi_A, \xi_Z, \xi)$$

- **Fields:** fermions, vector bosons, example of Feynman Rules

<u>vector boson propagators:</u>	$A : \sim\!\sim\!\sim\!\sim\!\sim\!\sim$ $\frac{1}{p^2} \left\{ \delta_{\mu\nu} + (\xi_A^2 - 1) \frac{p_\mu p_\nu}{p^2} \right\}$
$Z : \sim\!\sim\!\sim\!\sim\!\sim\!\sim$	$\frac{1}{p^2 + M_Z^2} \left\{ \delta_{\mu\nu} + (\xi_Z^2 - 1) \frac{p_\mu p_\nu}{p^2 + \xi_Z^2 M_Z^2} \right\}$
$W^\pm : \sim\!\sim\!\sim\!\sim\!\sim\!\sim$	$\frac{1}{p^2 + M_W^2} \left\{ \delta_{\mu\nu} + (\xi^2 - 1) \frac{p_\mu p_\nu}{p^2 + \xi^2 M_W^2} \right\}$

- Unphysical fields: $\phi^0, \phi^\pm, Y^A, Y^Z, X^\pm$, the physical H field.
- Passarino–Veltman (PV) functions and reduction:
Presently, SANC knows ALL up to third rank tensorial reduction of up to four-point PV functions: A_0, B_0, C_0 and D_0 ; and the so-called *special* PV functions: a_0, b_0, c_0 and d_0 , which are due to particular form of photonic propagator in R_ξ gauge (terms $\propto 1/p^4$).
- A **fortran library** for numerical calculation of these functions is created and thoroughly tested by means of comparison with the other codes.

2. Basic notions, contd.

Amplitude's basis, Scalar Form Factors (**SFF**), Helicity Amplitudes (**HA**)

Example of decays $B(Q) \rightarrow f(p_1)\bar{f}(p_2)$

$H \rightarrow f\bar{f}$ decay – $\mathcal{A} \propto I\mathcal{F}_S$

1 structure (**L–basis**), **1 SFF**, **1 HA**

$Z \rightarrow f\bar{f}$ decay – $\mathcal{A} \propto i\gamma_\mu\gamma_6\mathcal{F}_L + i\gamma_\mu\mathcal{F}_Q + m_f(p_1 - p_2)_\mu\mathcal{F}_D$

3 structures (**L,Q,D–basis**), **3 SFFs**, **3 HAs**

$W \rightarrow u\bar{d}$ decay – $\mathcal{A} \propto i\gamma_\mu\gamma_6\mathcal{F}_L + i\gamma_\mu\gamma_7\mathcal{F}_R + m_u(p_1 - p_2)_\mu\gamma_6\mathcal{F}_{LD} + m_d(p_1 - p_2)_\mu\gamma_7\mathcal{F}_{RD}$

4 structures (**L,R,LD,RD–basis**), **4 SFFs**, **4 HAs**

The **3 HAs** depend on kinematical factors, coupling constants and **3 SFFs**, example of Z decay:

$$\mathbf{A}_{0++}^Z = \mathbf{A}_{0--}^Z = \frac{gm_f}{c_W} \left[a_f \mathcal{F}_L + \delta_f \mathcal{F}_Q + \frac{1}{2} a_f \beta_f^2 M_Z^2 \mathcal{F}_D \right]$$

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$$\beta_f^2 = 1 - 4 \frac{m_f^2}{M_Z^2}, \quad \delta_f = v_f - a_f = -2Q_f s_W^2, \quad a_f = I_f^{(3)}.$$

3. Present Status of the project

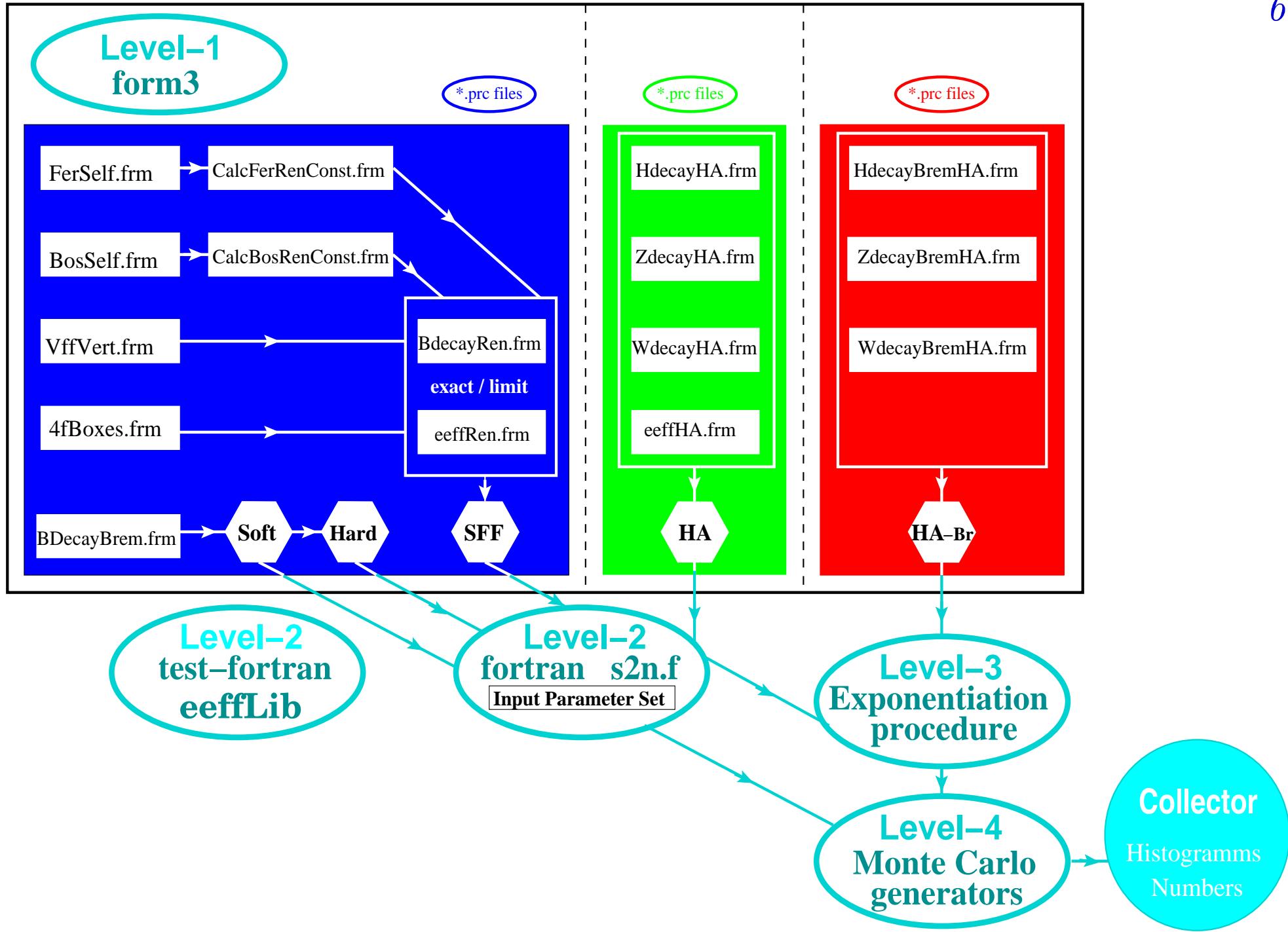
Basic information about SANC

- **Four-level computer system** for automatic calculation of pseudo- and realistic observables (decay rates, event distributions) for experiments at future colliders.

Flow chart illustrates how it works for simplest POs, $H(Z, W) \rightarrow f_1 \bar{f}_2$ decay rates:

1. from \mathcal{L}_{SM} to the Ultra Violet free helicity amplitudes (all in **form3**);
 - **calculation of Scalar Form Factors, SFF**;
 - **of the Soft and Hard photons contributions to the decay rates**;
 - **of Helicity Amplitudes for basic process, HA**;
 - **of Helicity Amplitudes for an accompanying Bremsstrahlung process, HA-Br**;
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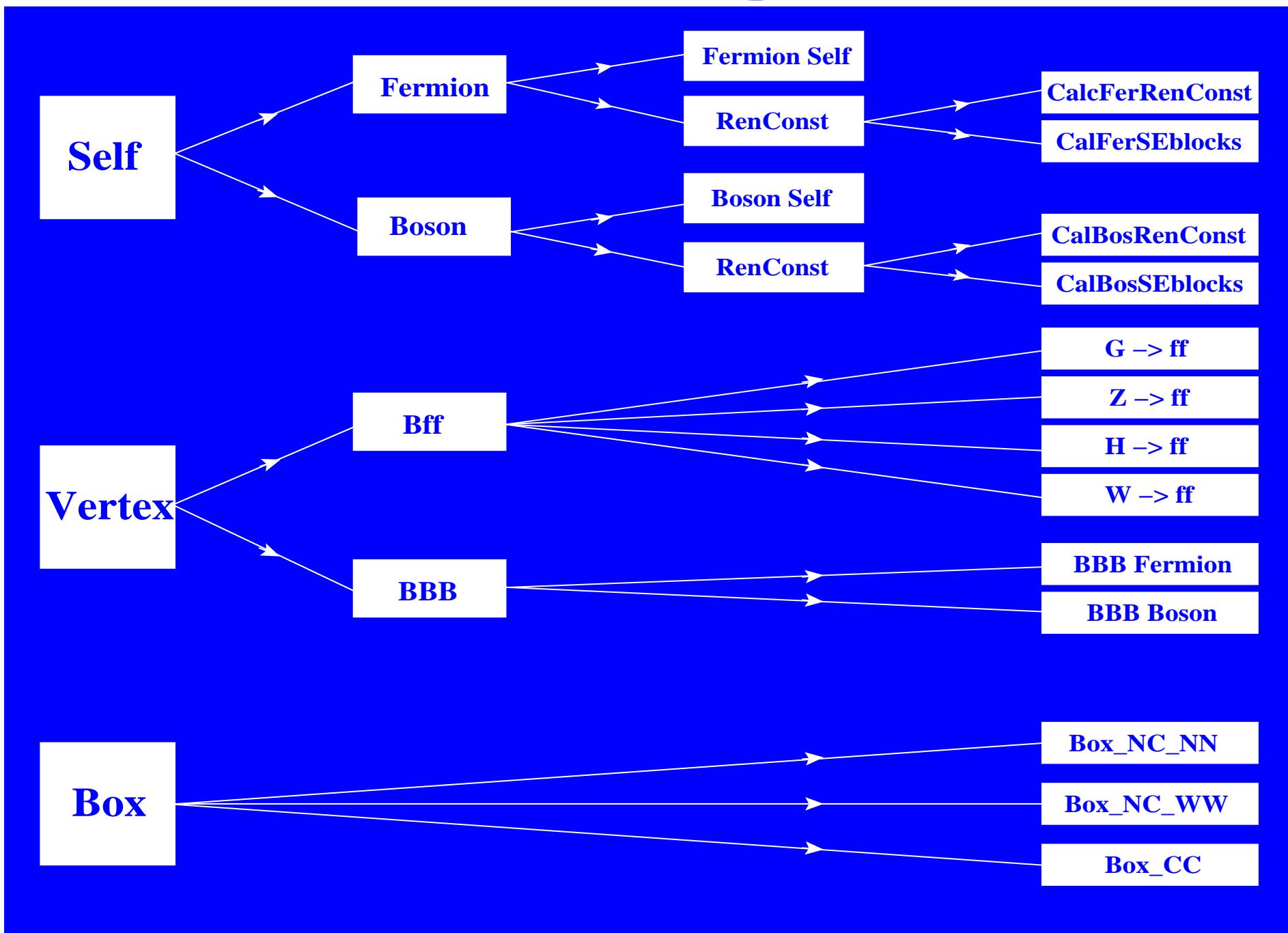
- **Internet based**
- **Database based**, i.e. a storage of source codes written in several languages, which talk to each other being placed into a homogeneous environment written in **JAVA** (linker).
- **PRECOMPUTATION**: one-loop diagrams could be precomputed and stored (to save CPU);
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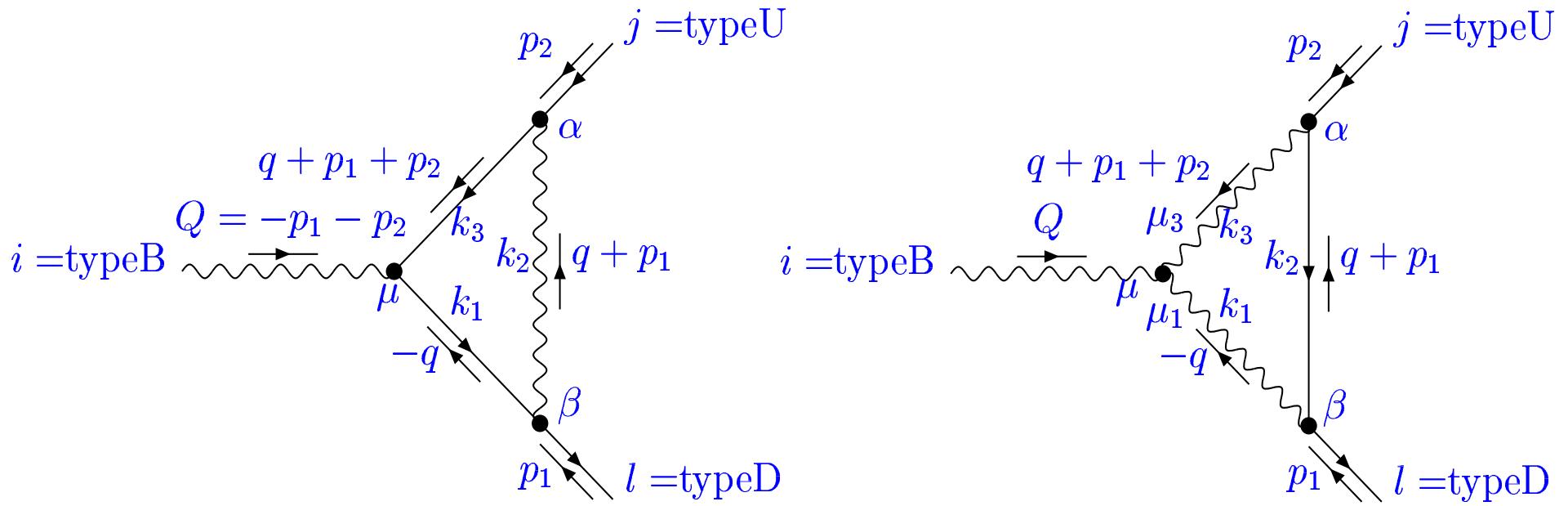
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*.prc files



An example of PRECOMPUTATION

Chain: Vertex → Bff → Z→ff

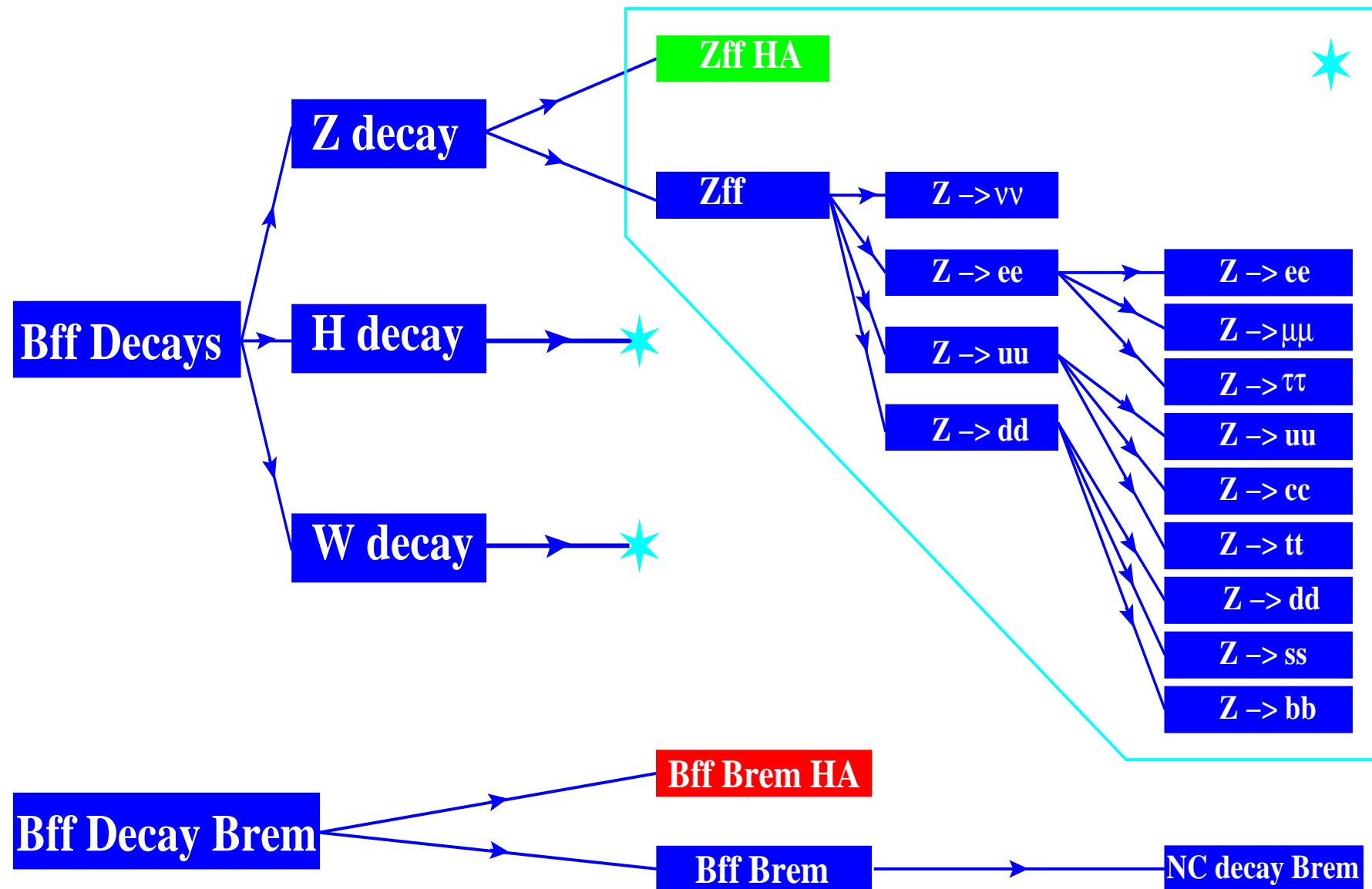


Vertices: FBF-topology,

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PROGRAMS

*,prc files *,prc files *.prc files



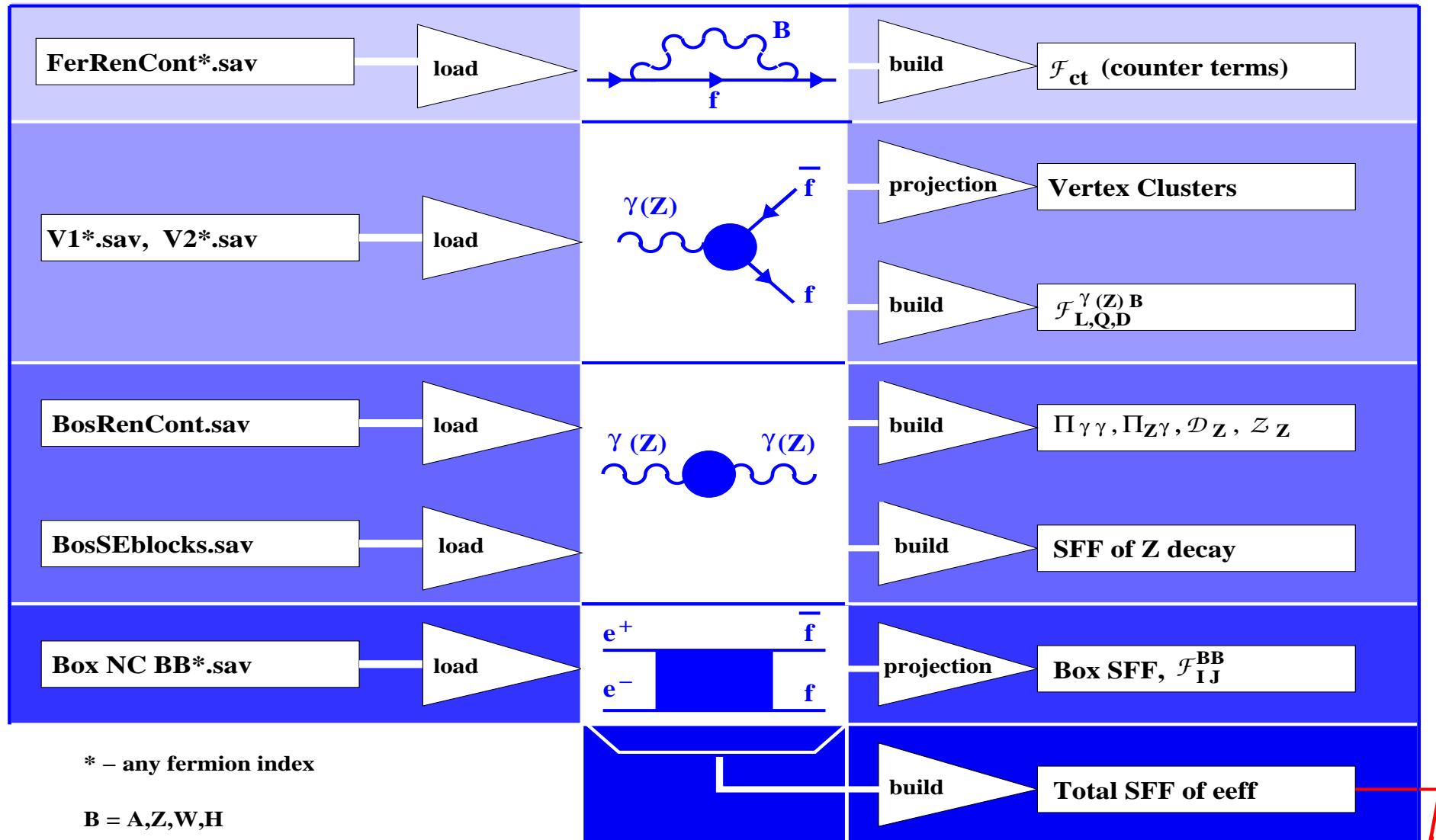
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 - several versions **v0.02c/d** – towards realization of levels 1,2,4 for decays $H(Z, W) \rightarrow f_1 \bar{f}_2$;
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Calculation flow in eeffRen.frm



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COMPARISON → AGREEMENT

$e^+e^- \rightarrow f\bar{f}$, ALL CHANNELS

- **eeffLib–ZFITTER**

SFFs → **8–9 digits**

Complete 1-loop differential cross section $d\sigma^{(1)}/d\cos\vartheta \rightarrow$ **7–8 digits**

Total 1-loop cross section and σ^{FB} for the light fermion masses → **6–7 digits**

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Complete 1-loop differential cross-sections $d\sigma^{(1)}/d\cos\vartheta \rightarrow$ **12–13 digits**

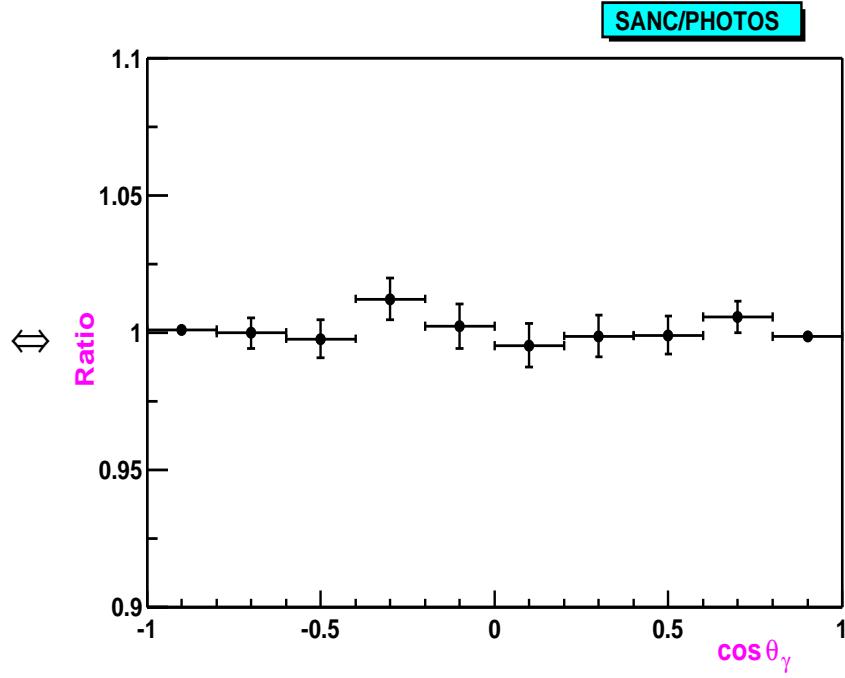
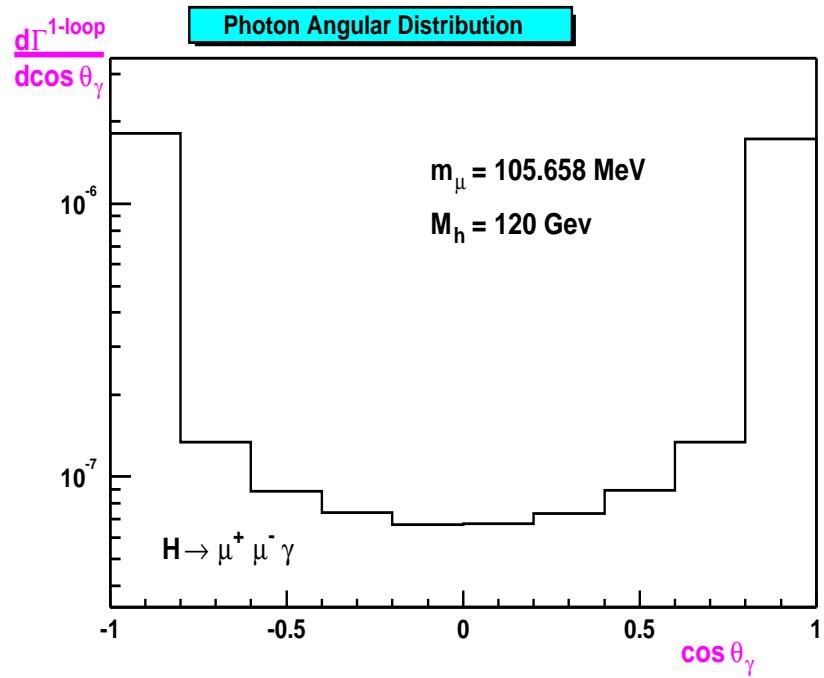
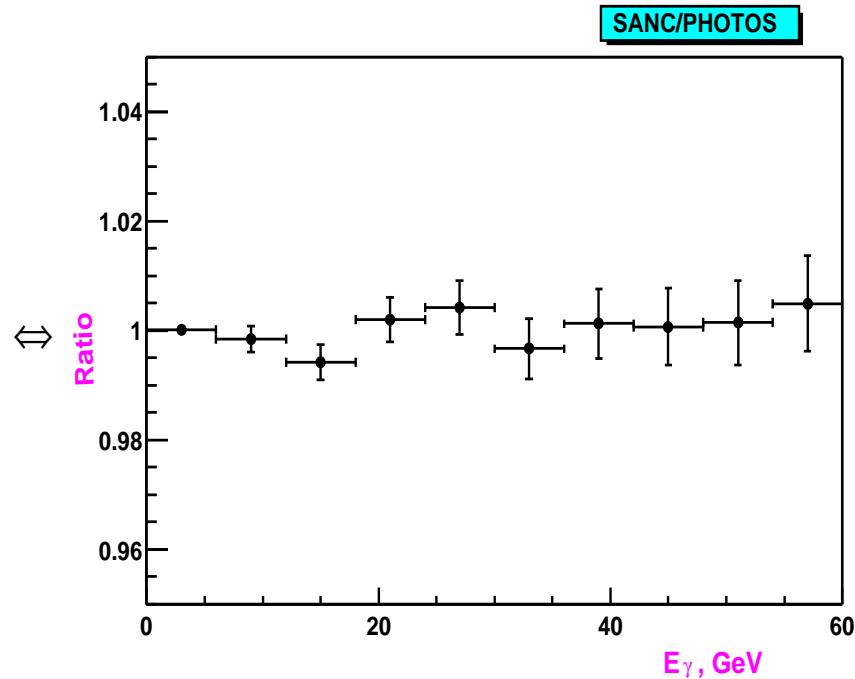
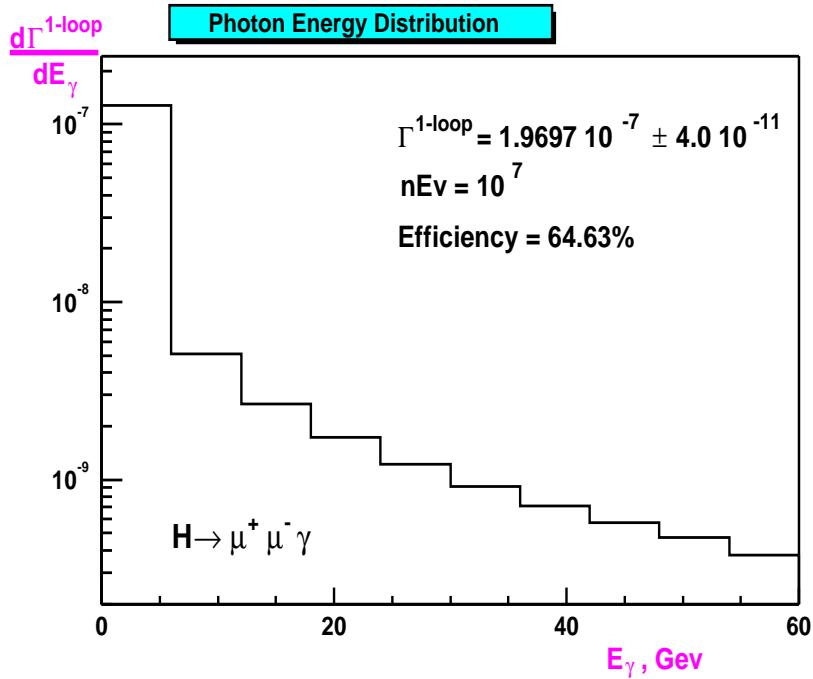
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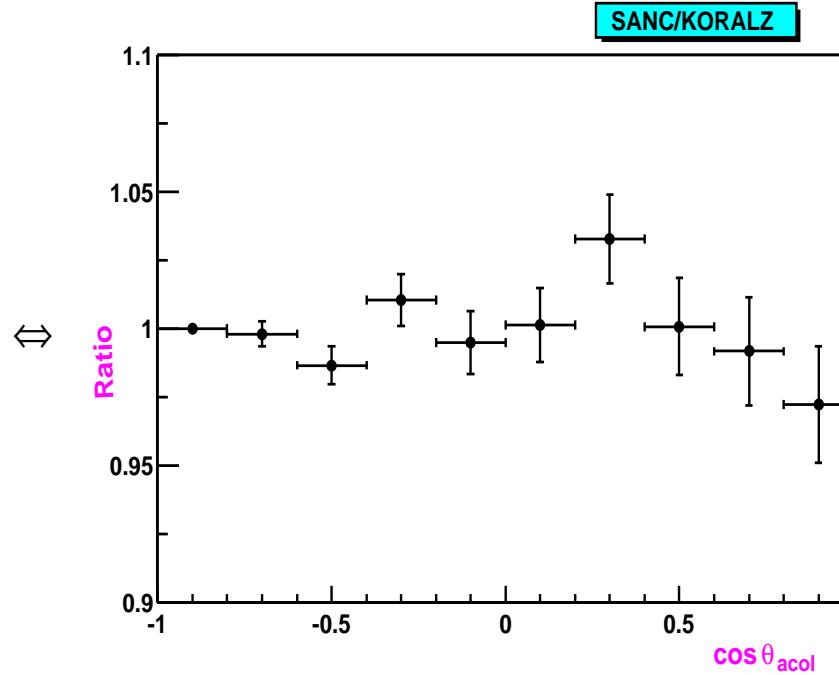
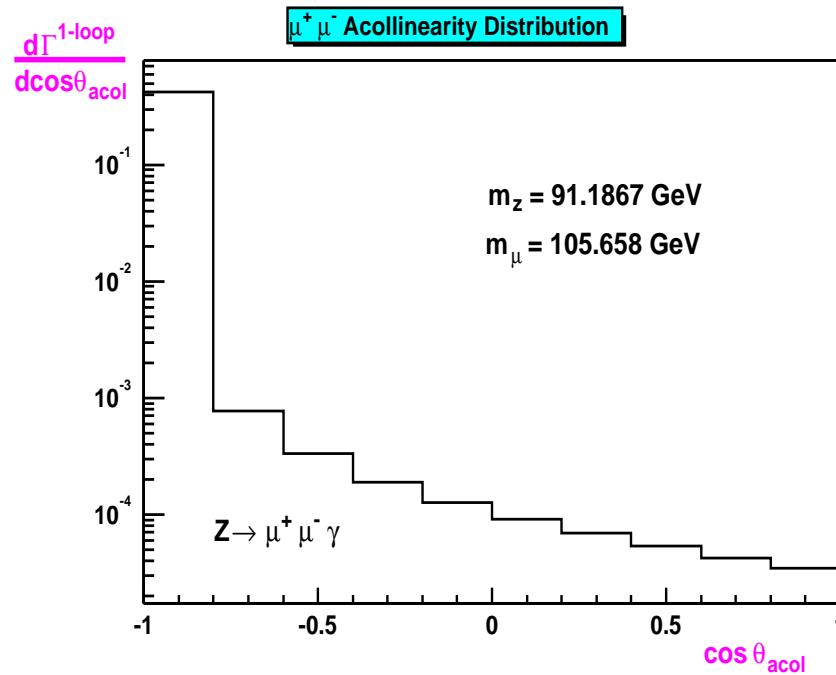
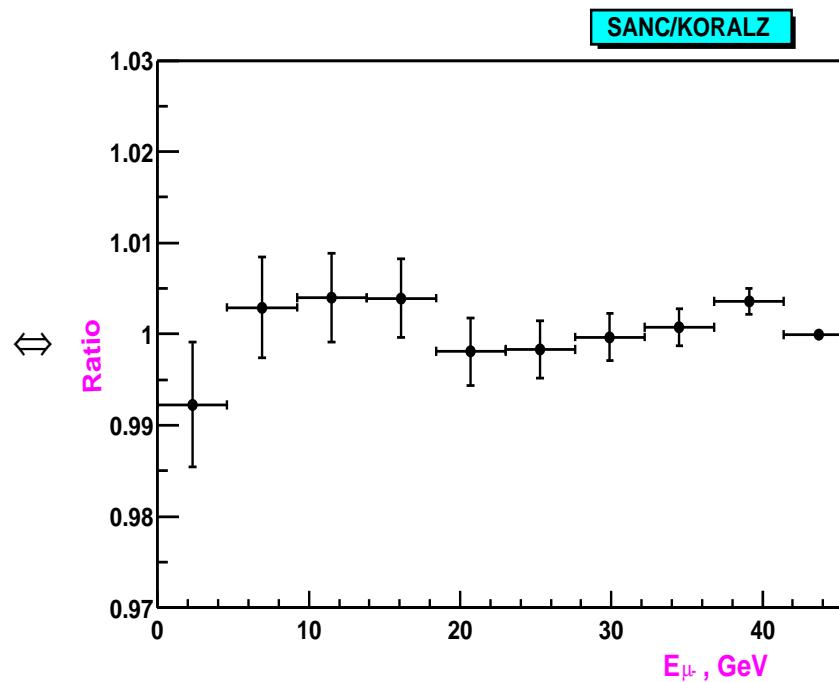
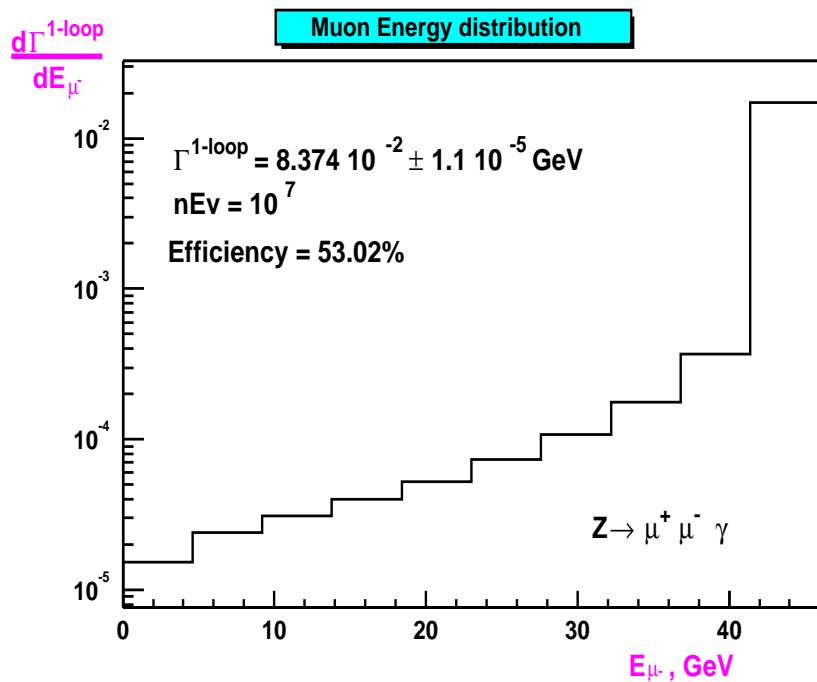
1-loop cross-section **without soft photons** → **11 digits**

- **s2n.f–topfit***

1-loop cross-section **with soft photons** → **8 digits**

* Bielefeld–Zeuthen group (hep-ph/0202102, J. Fleisher et al.)





4. Concluding remarks



ADDRESS <http://brg.jinr.ru/>

FIRST PHASE → release of *demonstration version 0.10* in 2002

SECOND PHASE → a complete software product, accessible via an Internet-based environment, and realizing the chain of calculations '**from the Lagrangian to the realistic distributions**' at the one-loop level, including

PROCESSES $2 \rightarrow 3$ and DECAYS $1 \rightarrow 4$

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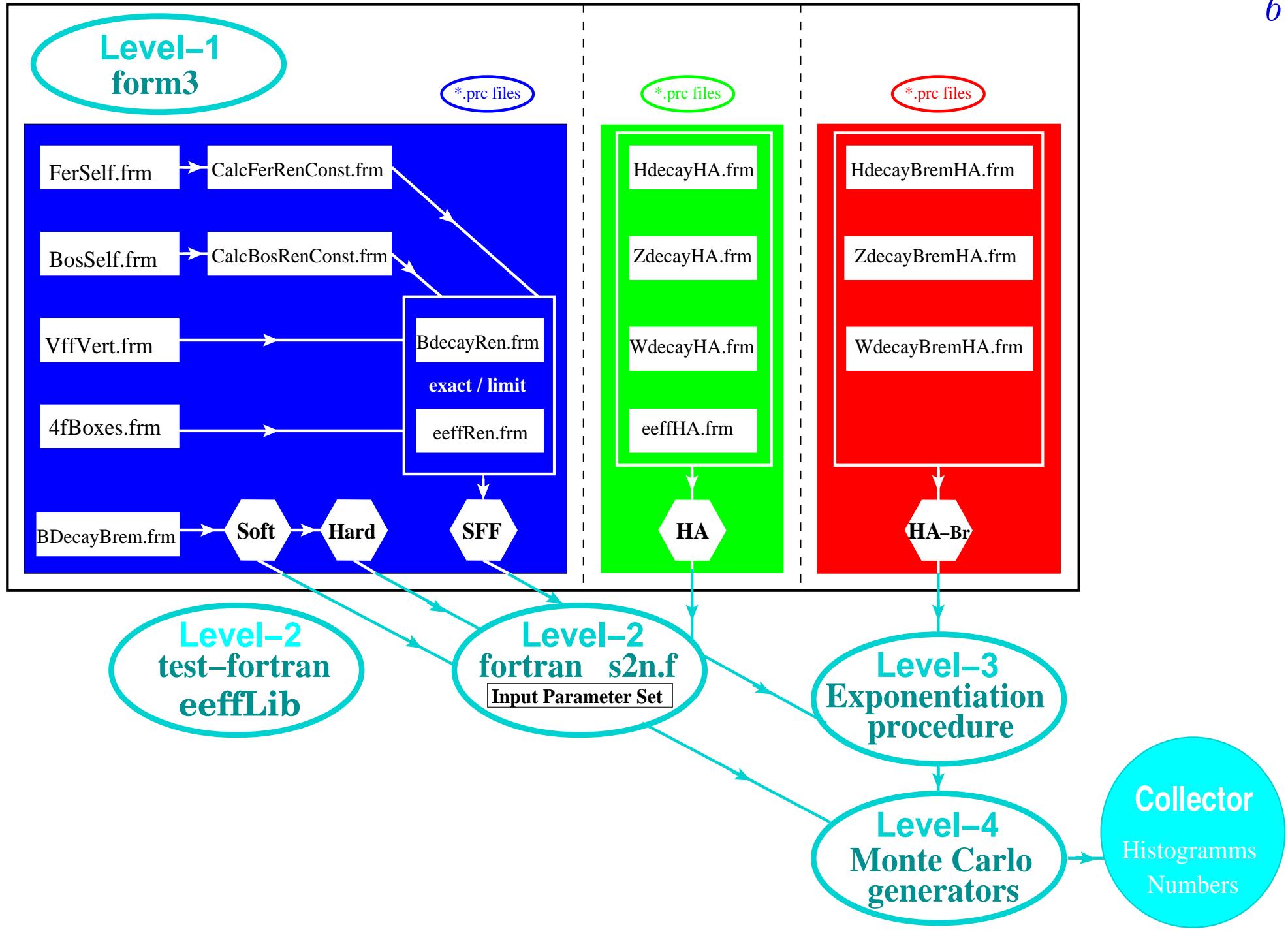
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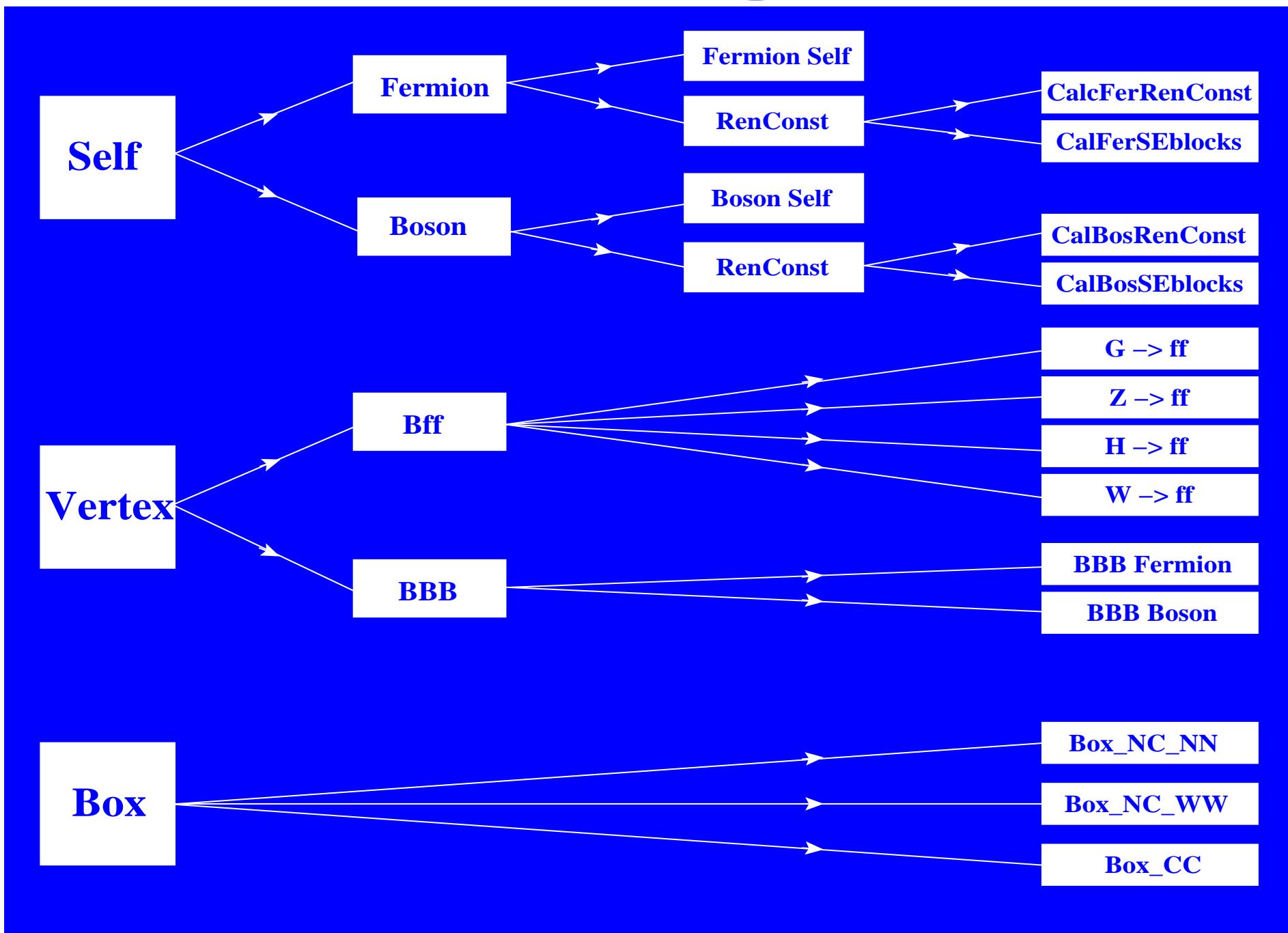
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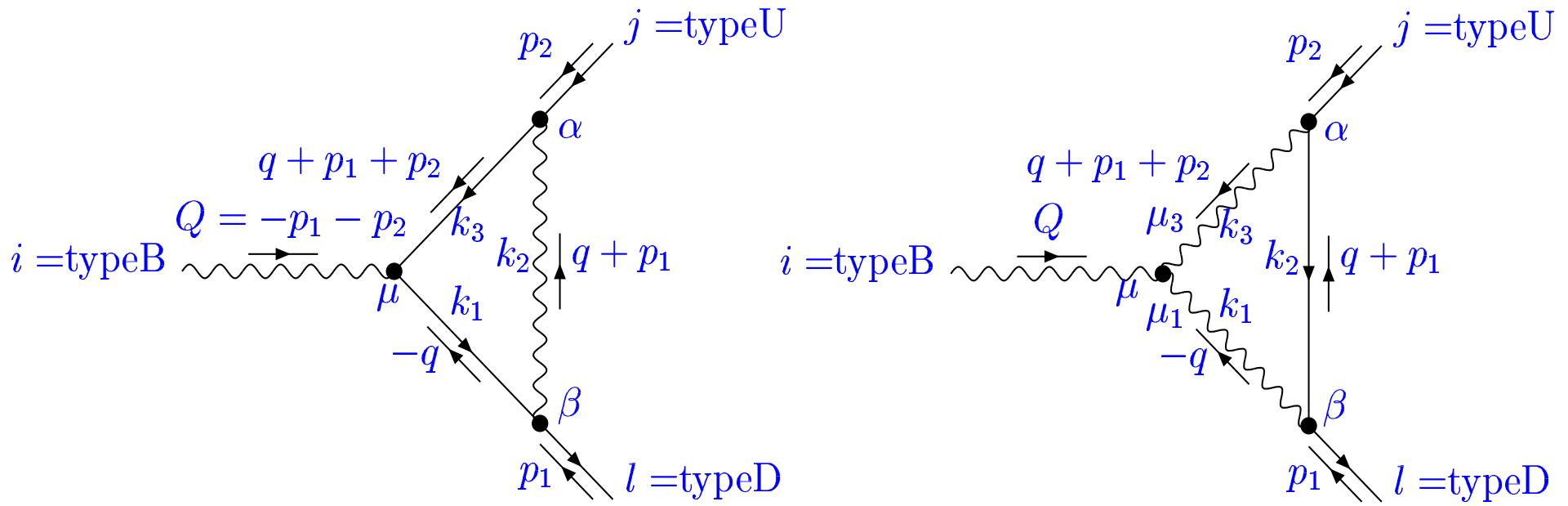
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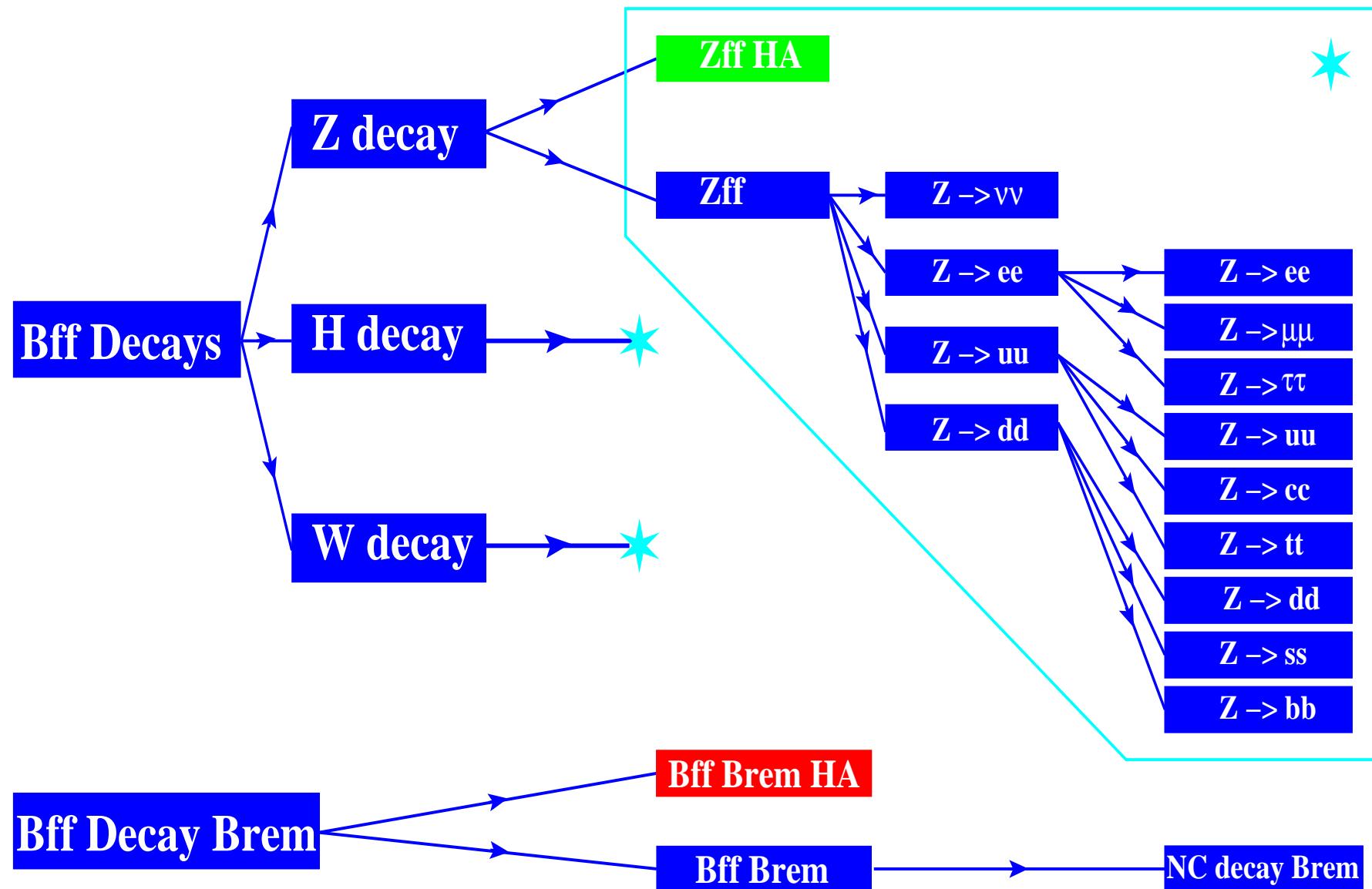


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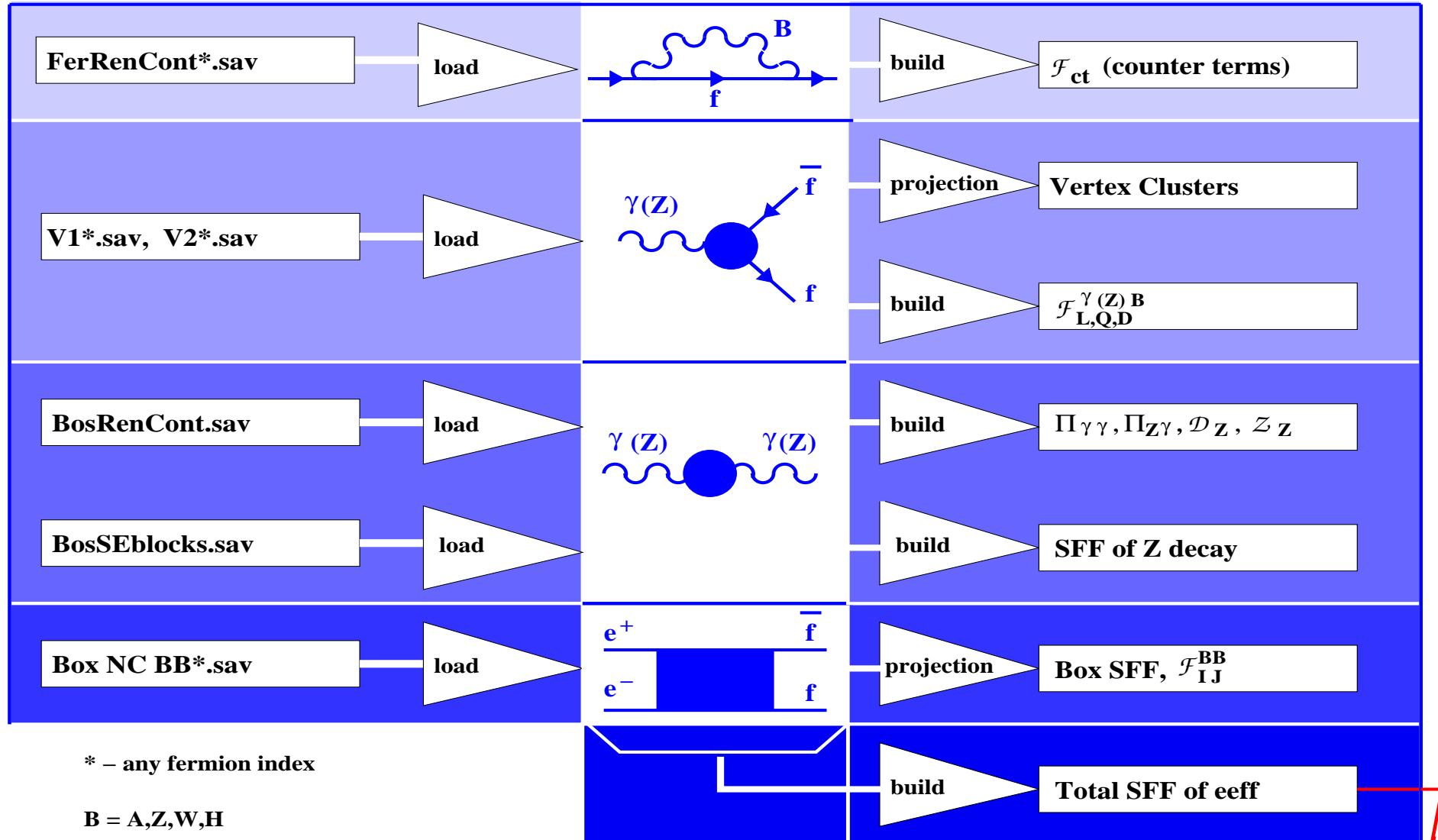
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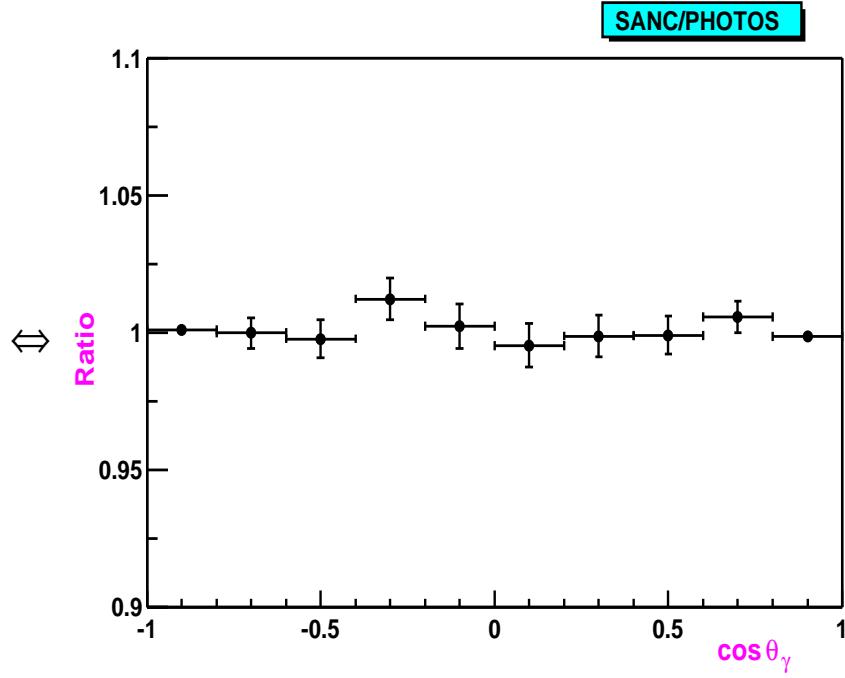
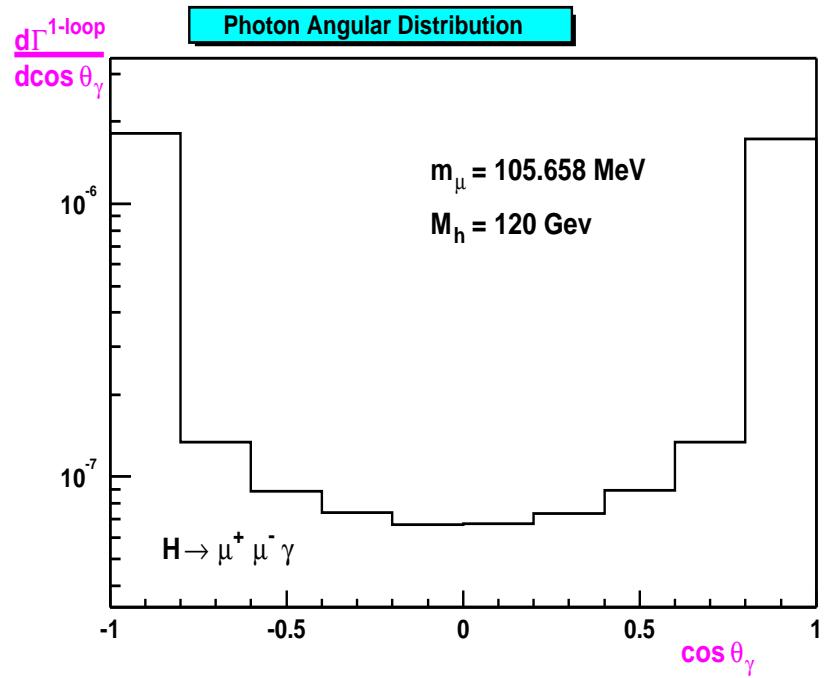
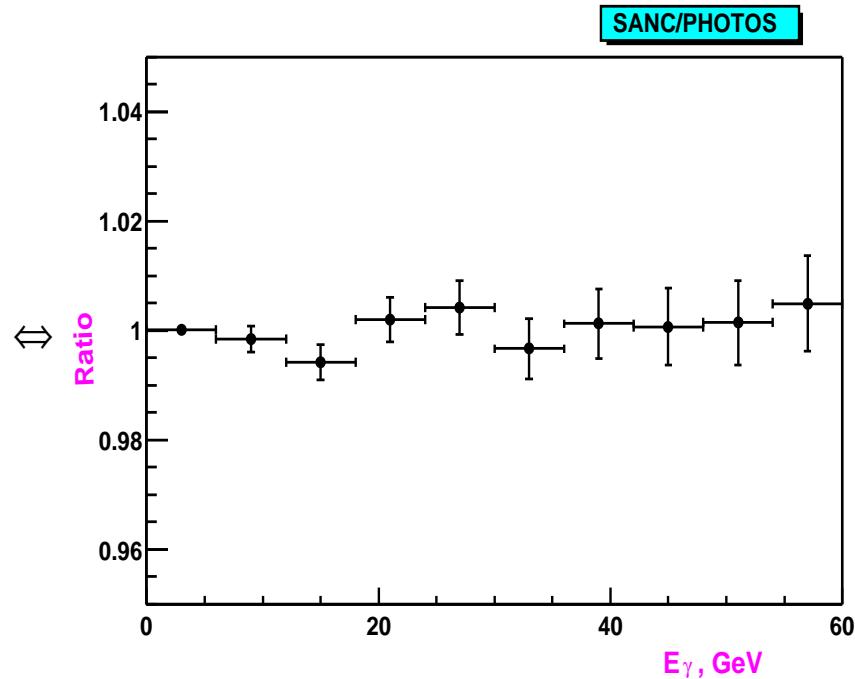
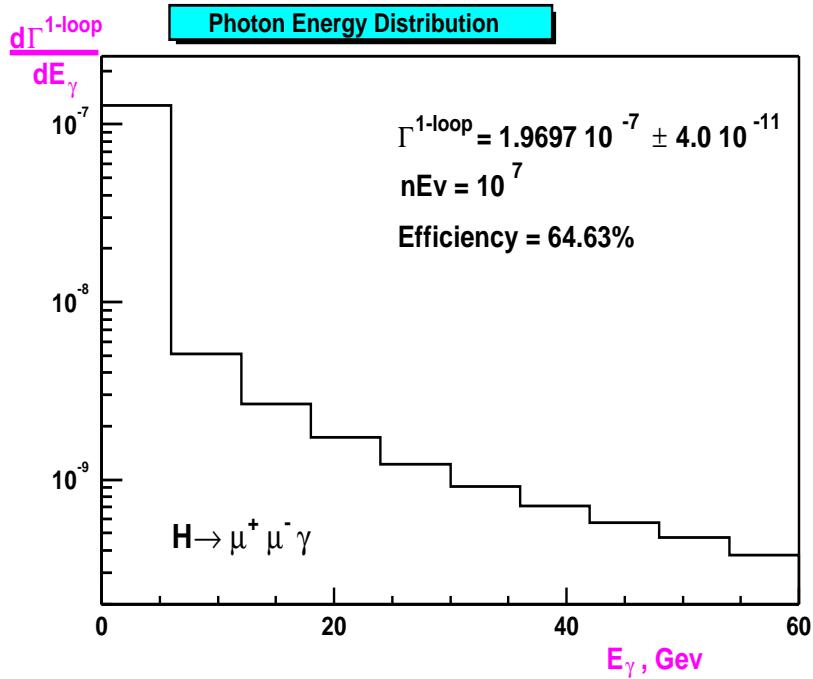
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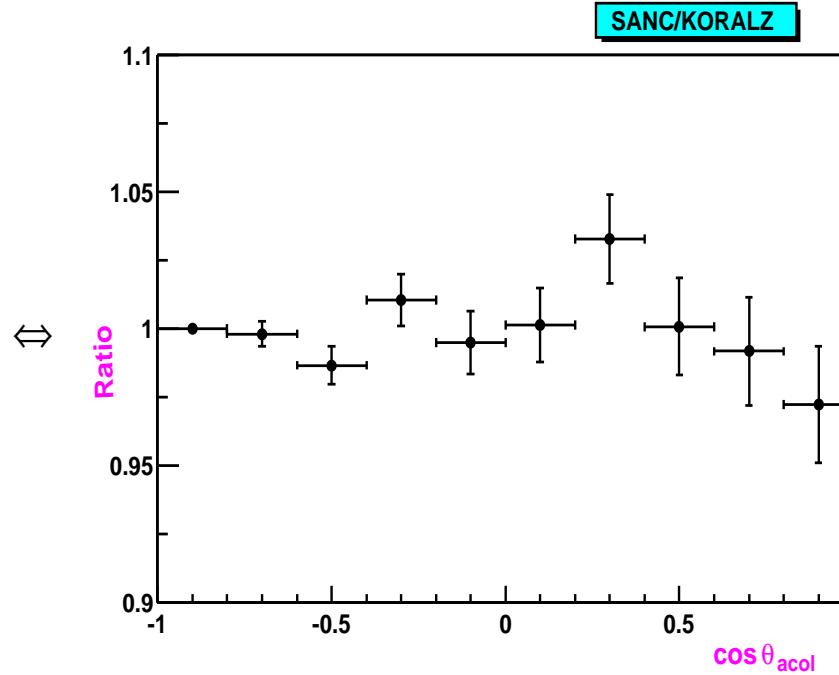
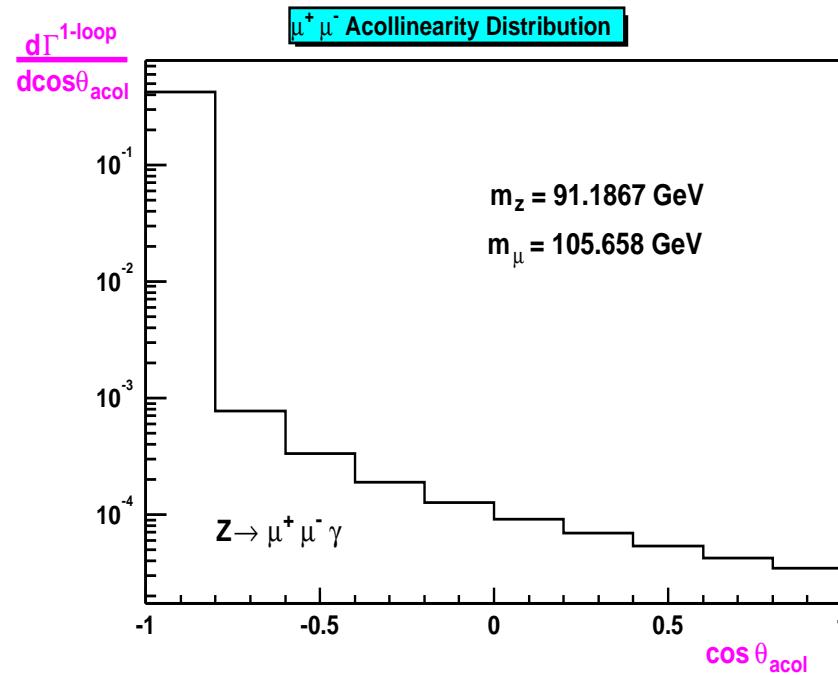
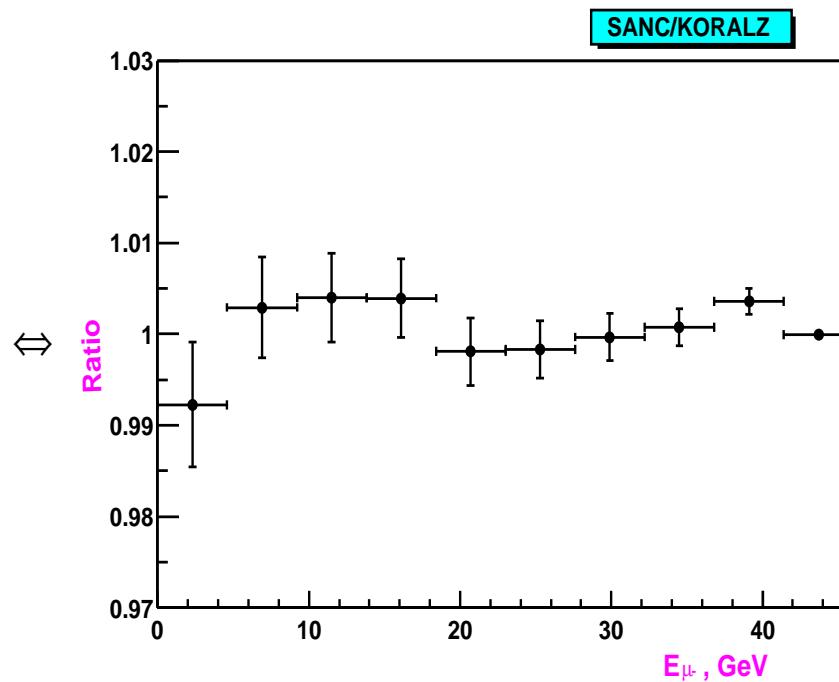
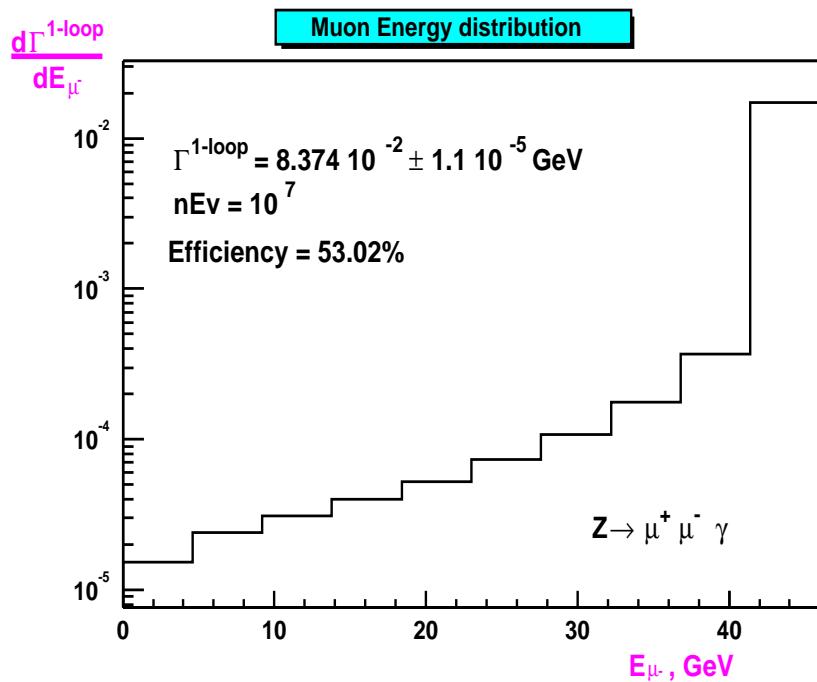
1-loop cross-section **without soft photons** → **11 digits**

- **s2n.f-topfit***

1-loop cross-section **with soft photons** → **8 digits**

* Bielefeld–Zeuthen group (hep-ph/0202102, J. Fleisher et al.)





4. Concluding remarks



ADDRESS <http://brg.jinr.ru/>

FIRST PHASE → release of *demonstration version 0.10* in 2002

SECOND PHASE → a complete software product, accessible via an Internet-based environment, and realizing the chain of calculations '**from the Lagrangian to the realistic distributions**' at the one-loop level, including

PROCESSES $2 \rightarrow 3$ and DECAYS $1 \rightarrow 4$